

**CHEM302**  
**Introduction to Computational**  
**Chemistry**

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“ $\psi$  ... is an oracle” – C. J. Cramer

$$\hat{H}\psi = E\psi$$

# Molecular Hamiltonian

$$\hat{\mathcal{H}} = - \sum_i \frac{1}{2} \nabla_i^2 - \sum_k \frac{1}{2} \nabla_k^2 - \sum_i \sum_k \frac{Z_k}{r_{ik}} + \sum_{i < j} \frac{1}{r_{ij}} + \sum_{k < l} \frac{Z_k Z_l}{r_{kl}}$$

# Variational Principle

# Born-Oppenheimer Approximation

$$\Psi = \psi_1(1)\psi_2(2)\dots\psi_N(N)$$

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$$-\Psi = P(\Psi)$$

$$\Psi = \frac{1}{\sqrt{N!}} \begin{vmatrix} \chi_1(1) & \chi_2(1) & \dots & \chi_N(1) \\ \chi_1(2) & \chi_2(2) & \dots & \chi_N(2) \\ \vdots & \vdots & \ddots & \vdots \\ \chi_1(N) & \chi_2(N) & \dots & \chi_N(N) \end{vmatrix}$$

# Self-consistent field (SCF)

